

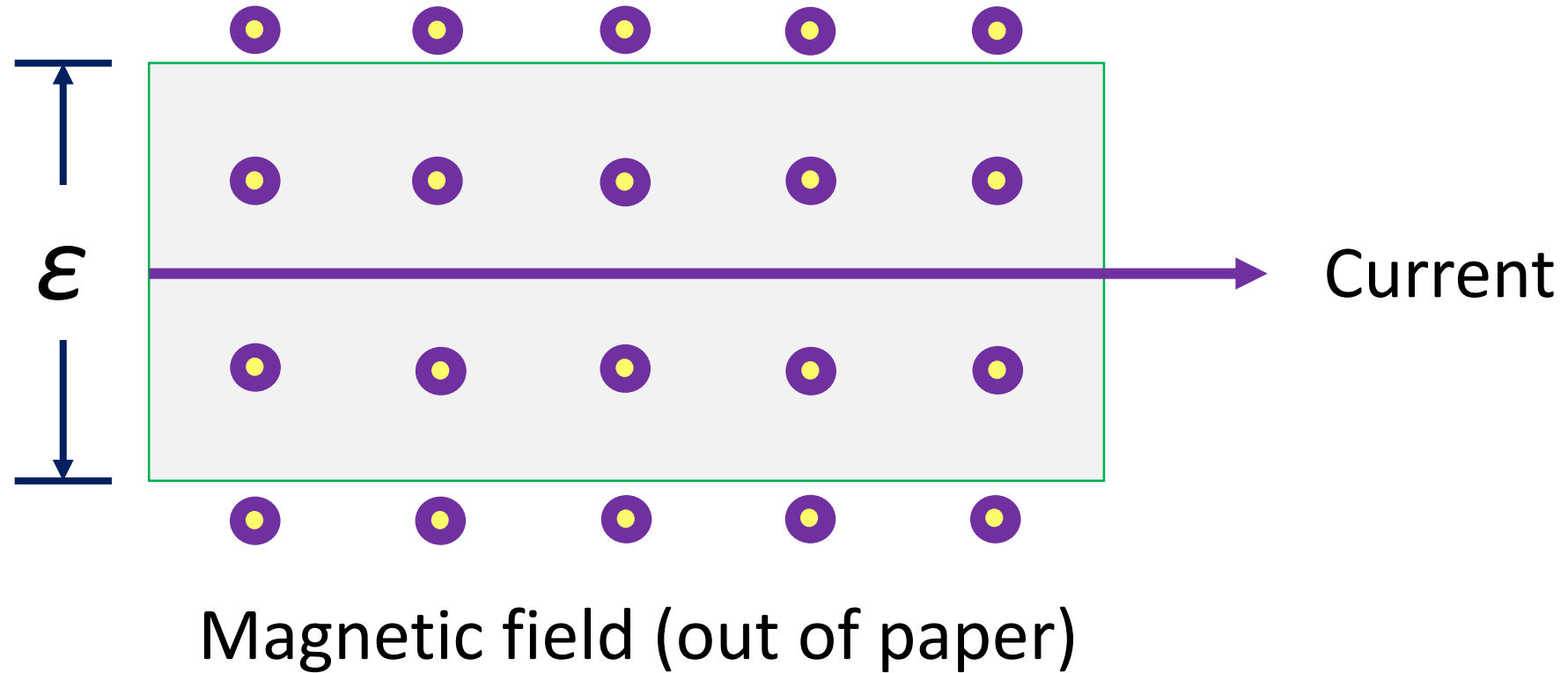
# Hall effect

$$V_H = - \left( \frac{1}{nq} \right) \frac{I_x B_z}{t}$$

Dr Mohammad Abdur Rashid



# Hall effect

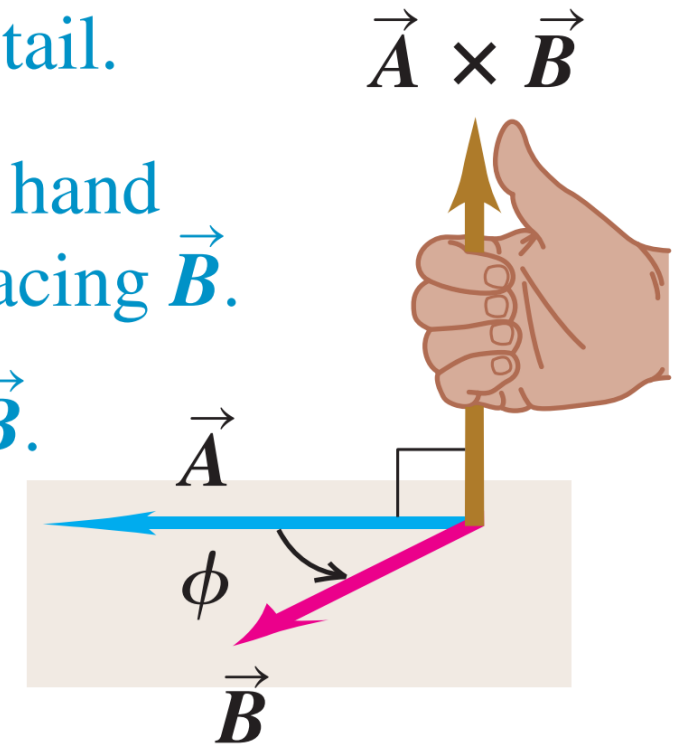


# Right-hand rule

The vector product  $\vec{A} \times \vec{B}$  determined by the right-hand rule.

$$\vec{B} \times \vec{A} = -\vec{A} \times \vec{B}$$

- ① Place  $\vec{A}$  and  $\vec{B}$  tail to tail.
- ② Point fingers of right hand along  $\vec{A}$ , with palm facing  $\vec{B}$ .
- ③ Curl fingers toward  $\vec{B}$ .
- ④ Thumb points in direction of  $\vec{A} \times \vec{B}$ .



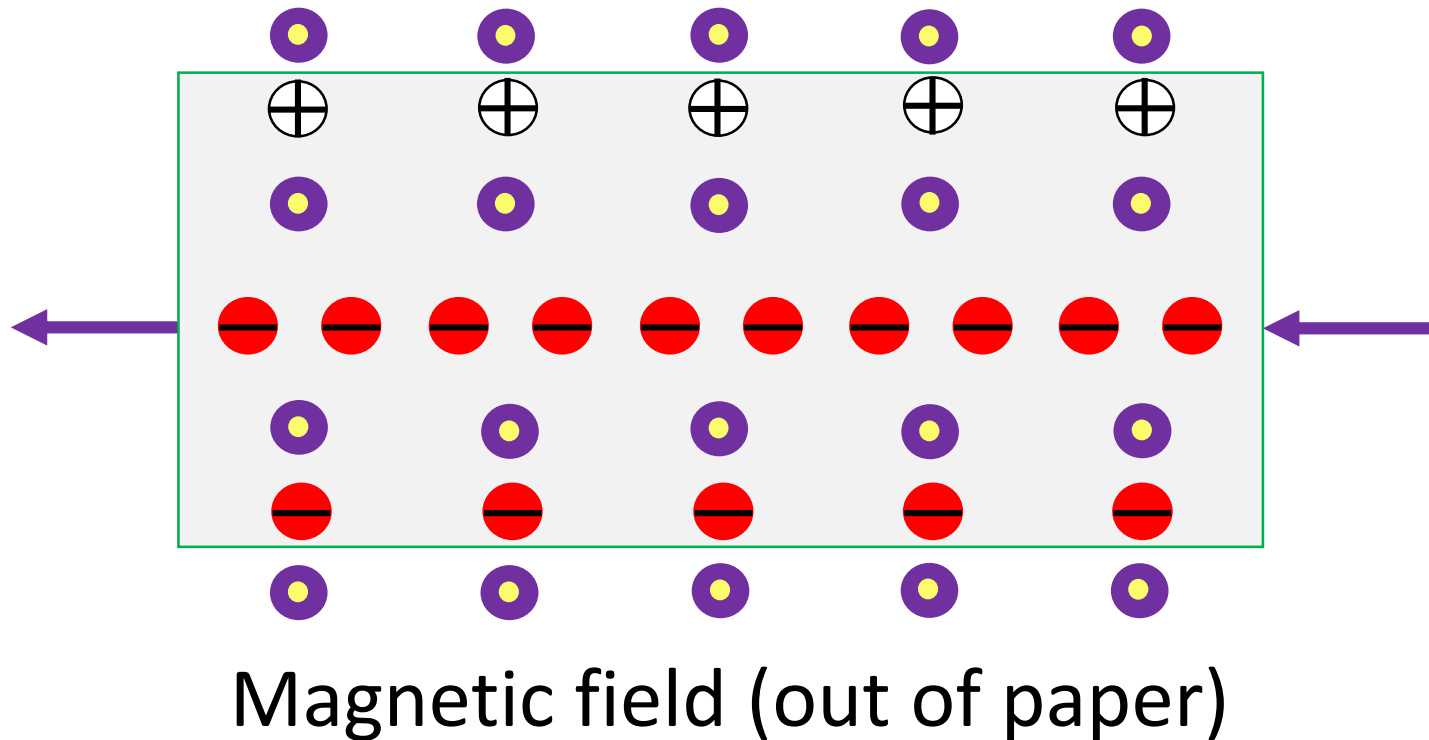
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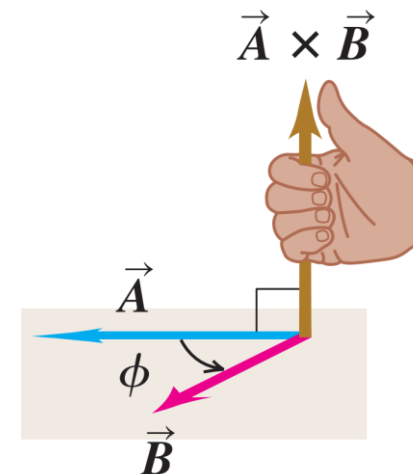
# Magnetic force on moving electrons

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$\mathbf{F} = -e(\mathbf{v} \times \mathbf{B})$$

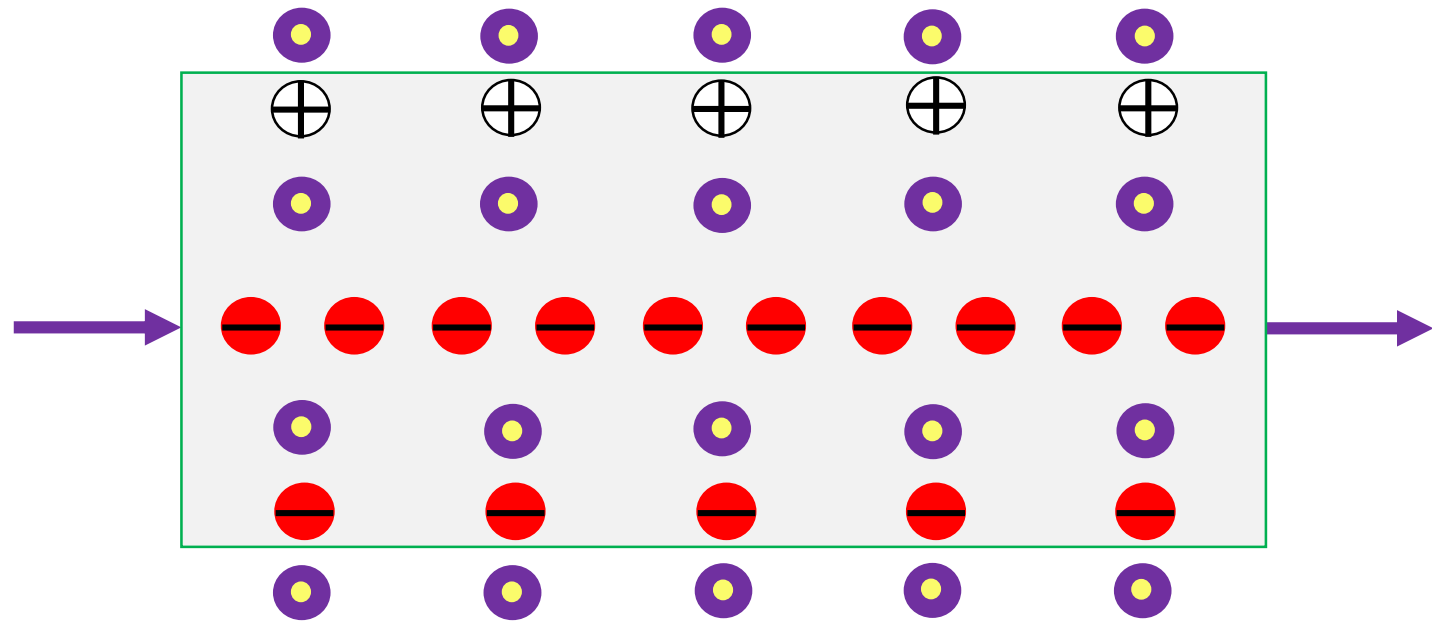


Motion of electrons



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# Magnetic force on moving electrons

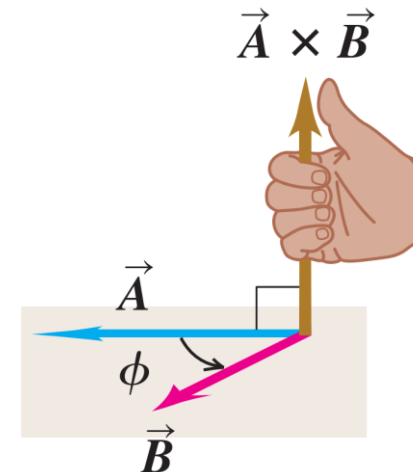


Magnetic field (out of paper)

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$\mathbf{F} = -e(\mathbf{v} \times \mathbf{B})$$

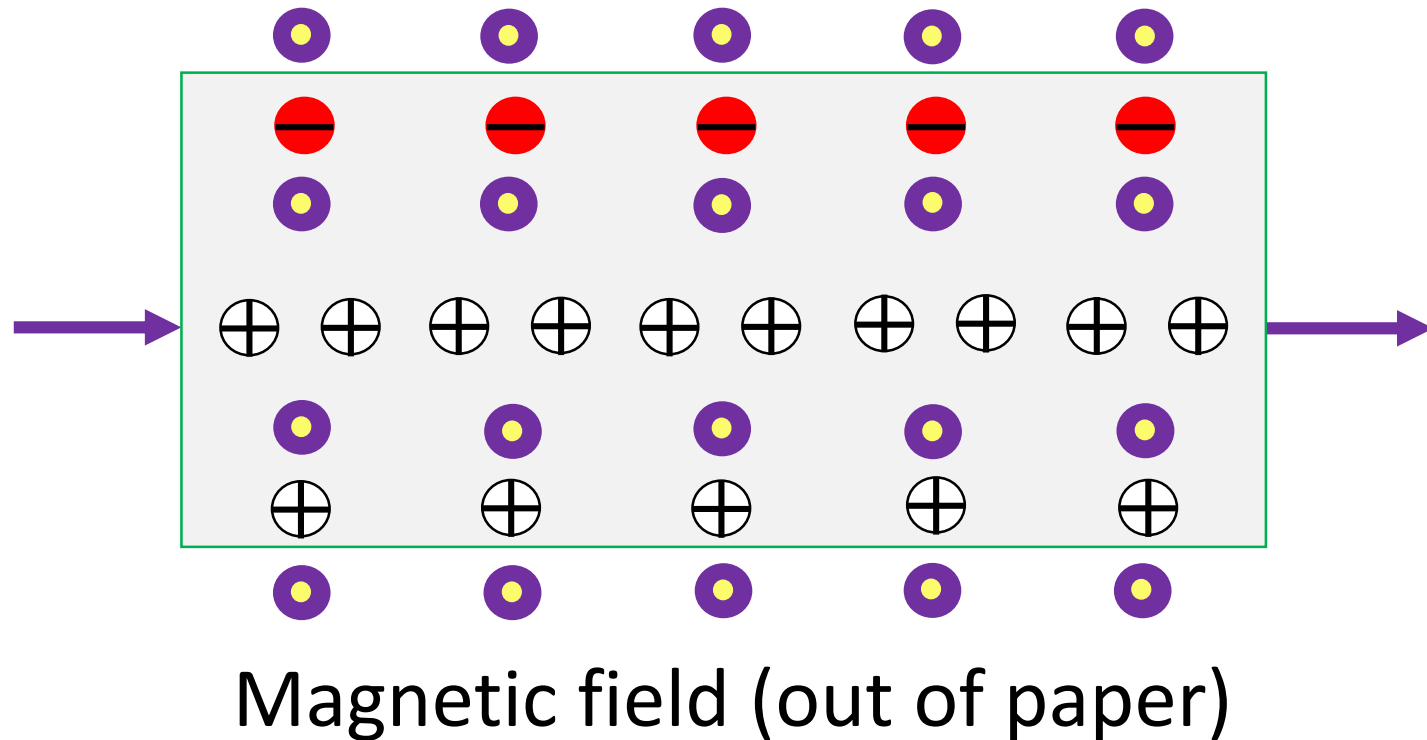
Direction of current



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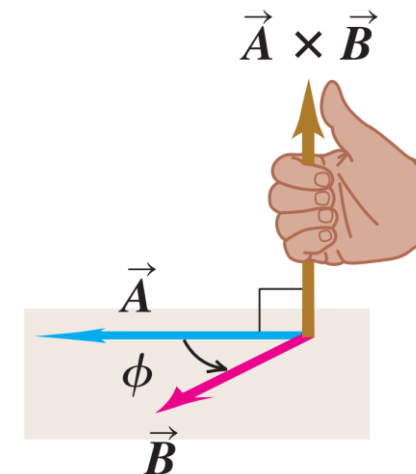
# Magnetic force on moving holes



$$e = 1.6 \times 10^{-19} \text{ C}$$

$$\mathbf{F} = e(\mathbf{v} \times \mathbf{B})$$

Direction of current



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# Magnetic force on moving holes

$e = 1.6 \times 10^{-19} \text{ C}$

$\mathbf{F} = e(\mathbf{v} \times \mathbf{B})$

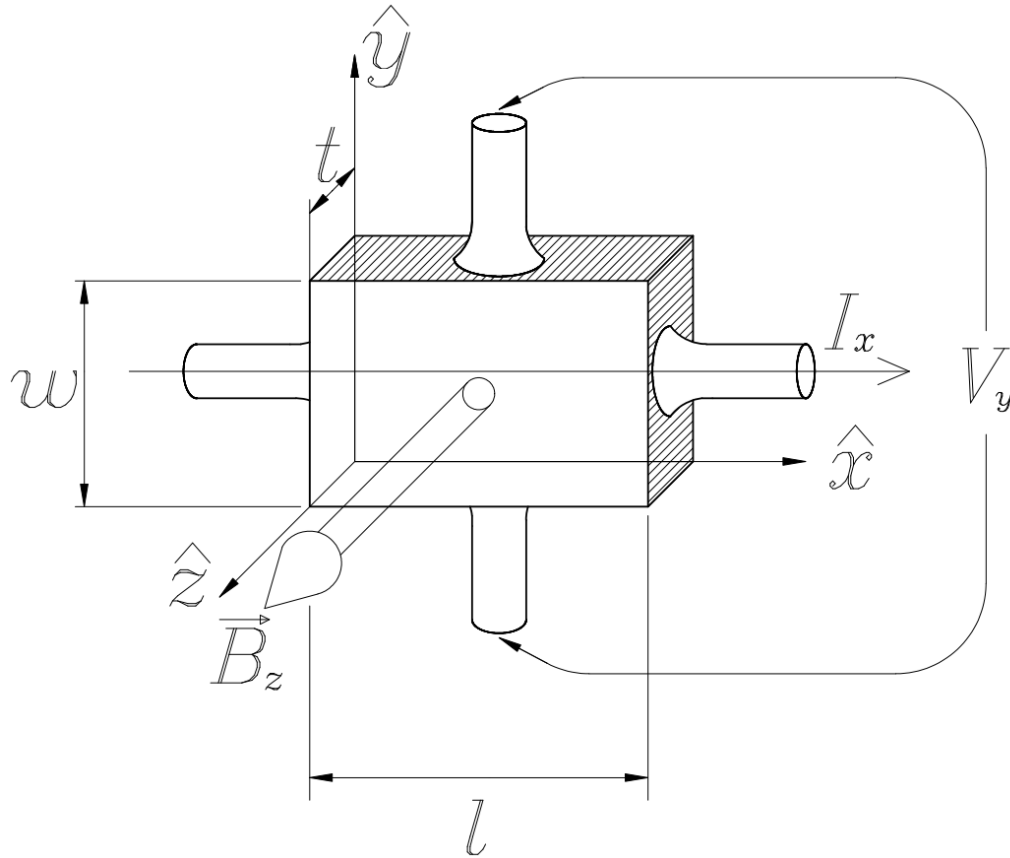
Direction of current

Magnetic field (out of paper)

$\mathbf{B}$   $\mathbf{F}_+$   $\mathbf{v}$

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# Hall voltage



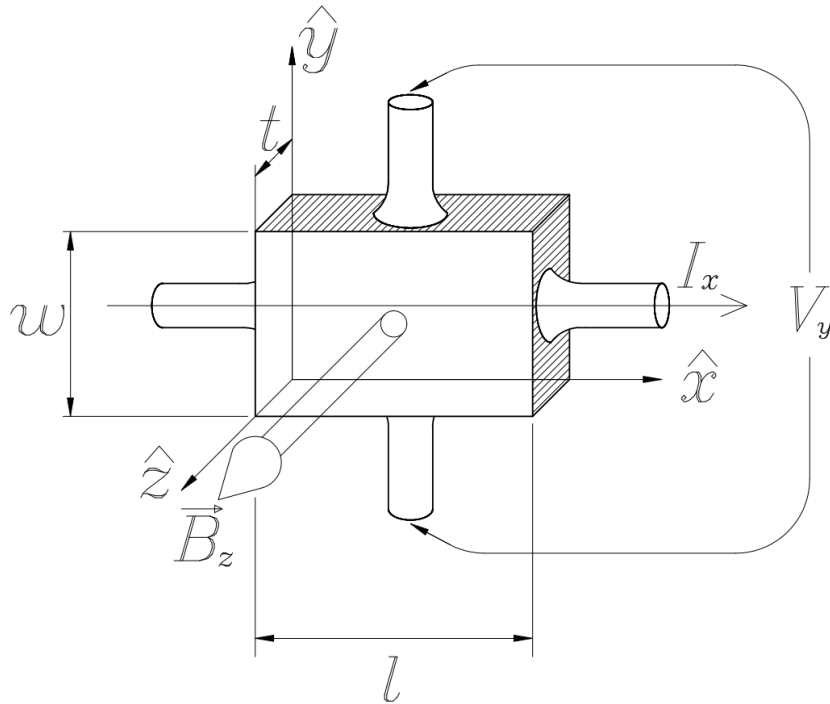
[http://courses.washington.edu/phys431/hall\\_effect/hall\\_effect.pdf](http://courses.washington.edu/phys431/hall_effect/hall_effect.pdf)

Assume the conductor to have charge carrier of charge  $q$  (can be either positive or negative or both, but we take it to be of just one sign here), charge carrier number density  $n$  (i.e., number of carriers per unit volume), and charge carrier drift velocity  $v_x$  when a current  $I_x$  flows in the positive  $x$  direction.





# Hall voltage

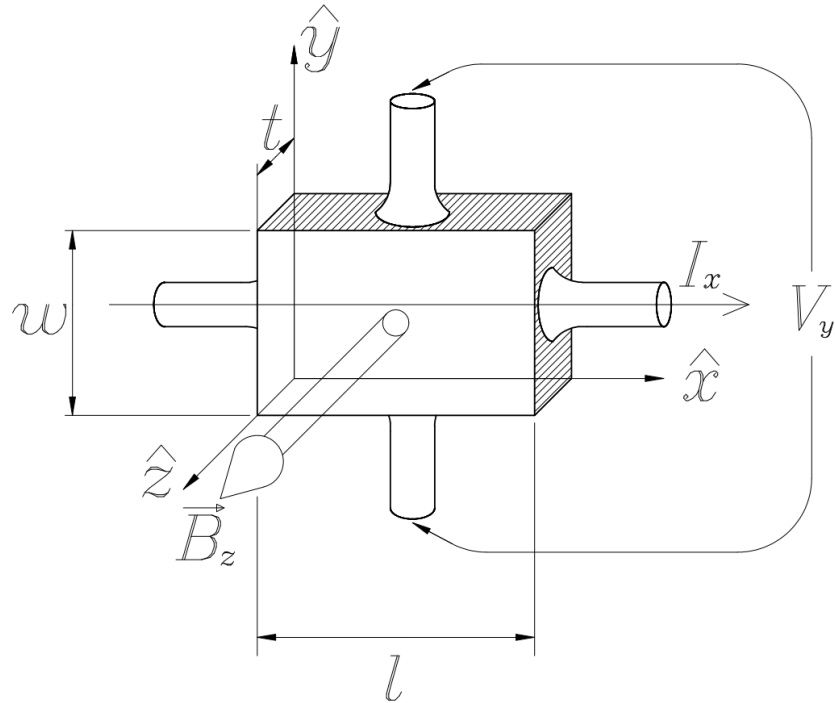


The charge carriers will experience a Lorentz force  $q(\mathbf{v} \times \mathbf{B})$  that will deflect them toward one side of the slab. The result of this deflection is to cause an accumulation of charges along one side of the slab which creates a transverse electric field  $E_y$  that counteracts the force of the magnetic field.

[http://courses.washington.edu/phys431/hall\\_effect/hall\\_effect.pdf](http://courses.washington.edu/phys431/hall_effect/hall_effect.pdf)



# Hall voltage



When steady state is reached, there will be no net flow of charge in the  $y$  direction, since the electrical and magnetic forces on the charge carriers in that direction must be balanced. Since the force of an electric field on a charge  $q$  is  $q\mathbf{E}$ , we have

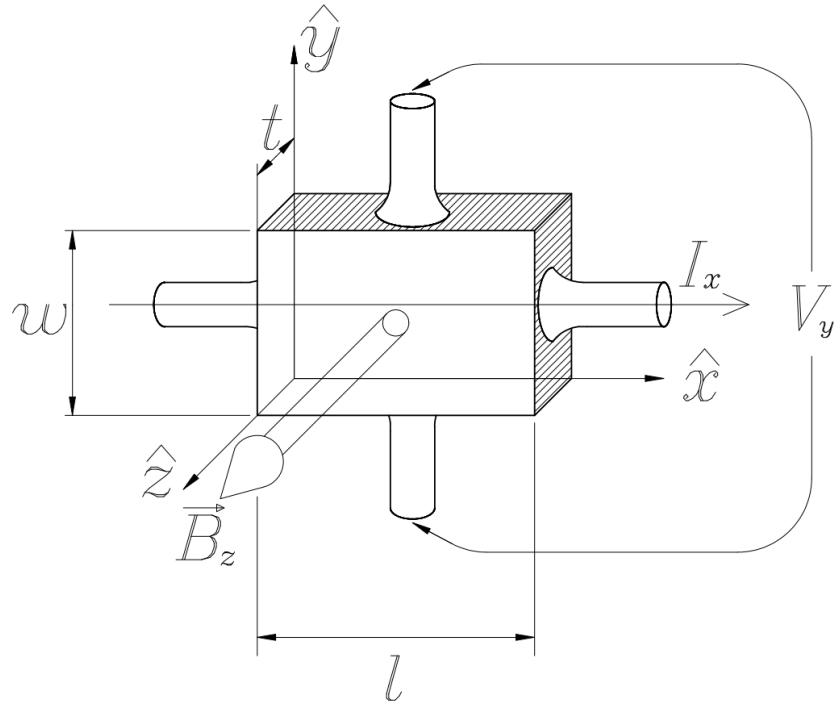
$$q\mathbf{E} = q(\mathbf{v} \times \mathbf{B})$$

$$E_y = v_x B_z$$

[http://courses.washington.edu/phys431/hall\\_effect/hall\\_effect.pdf](http://courses.washington.edu/phys431/hall_effect/hall_effect.pdf)



# Hall voltage



[http://courses.washington.edu/phys431/hall\\_effect/hall\\_effect.pdf](http://courses.washington.edu/phys431/hall_effect/hall_effect.pdf)

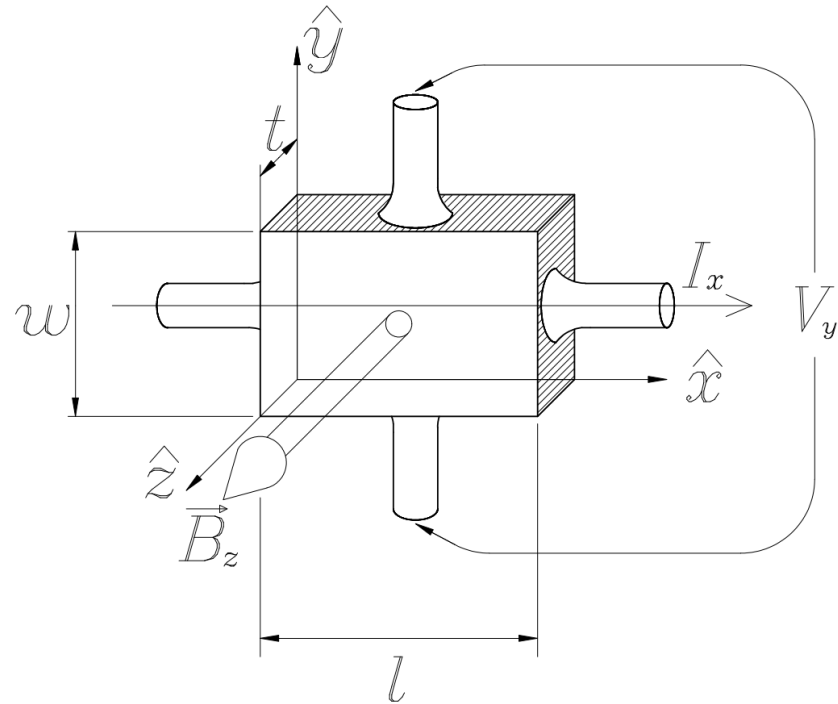
The potential difference across the sample — the Hall voltage  $V_H$  — which is related to the Hall field by

$$\begin{aligned} V_H &= -E_y w \\ &= -v_x w B_z \end{aligned}$$

The current  $I_x$  is related to the charge density  $nq$  and the drift velocity  $v_x$  as

$$I_x = nq v_x w t$$

# Hall voltage



[http://courses.washington.edu/phys431/hall\\_effect/hall\\_effect.pdf](http://courses.washington.edu/phys431/hall_effect/hall_effect.pdf)

$$V_H = - \left( \frac{1}{nq} \right) \frac{I_x B_z}{t}$$

$$\text{The Hall coefficient: } R_H = \frac{1}{nq}$$

It is positive if the charge carriers are positive, and negative if the charge carriers are negative. In practice, the polarity of  $V_H$  determines the sign of the charge carriers.



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