The Postulates of Quantum Mechanics

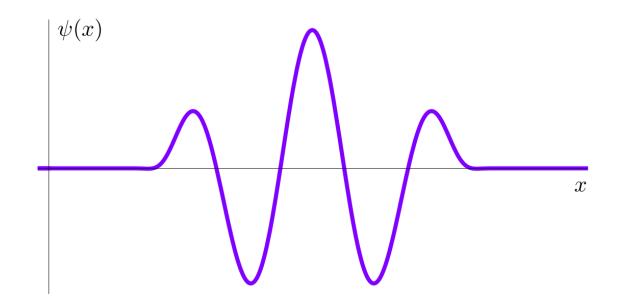
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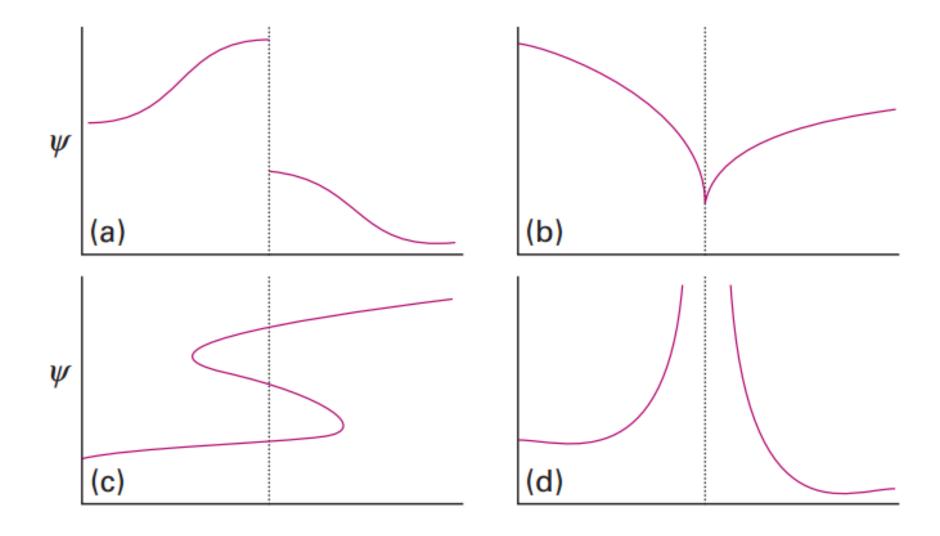
The wavefunction: All dynamical information is contained in the wavefunction ψ for the system, which is a mathematical function found by solving the Schrödinger equation for the system. In one dimension:

$$-\frac{\hbar^2}{2m}\frac{\mathrm{d}^2\psi}{\mathrm{d}x^2} + V(x)\psi = E\psi$$

The Born interpretation: If the wavefunction of a particle has the value ψ at some point r, then the probability of finding the particle in an infinitesimal volume $d\tau = dxdydz$ at that point is proportional to $|\psi|^2 d\tau$.

Acceptable wavefunctions: An acceptable wavefunction must be single-valued, continuous, not infinite over a finite region of space, and have a continuous slope.







Operators in QM

Observables: Observables, Ω , are represented by operators, $\hat{\Omega}$, built from the following position and momentum operators:

$$\hat{x} = x \times \qquad \hat{p}_x = \frac{\hbar}{i} \frac{d}{dx}$$

Uncertainty Principle

The Heisenberg uncertainty relation: It is impossible to specify simultaneously, with arbitrary precision, both the momentum and the position of a particle and, more generally, any pair of observables with operators that do not commute.

$$\Delta x \, \Delta p_x \geq \frac{\hbar}{2}$$

Postulate 1. The state of a quantum-mechanical system is completely specified by a wavefunction Ψ that depends on the coordinates and time. The square of this function $\Psi^*\Psi$ gives the probability density for finding the system with a specified set of coordinate values.

The wavefunction must be single-valued, finite and continuous.

$$\int \Psi^* \Psi \, d\tau = 1$$

Postulate 2. Every observable in quantum mechanics is represented by a linear, hermitian operator.

A linear operator is one which satisfies the identity $\hat{A}(c_1\psi_1 + c_2\psi_2) = c_1\hat{A}\psi_1 + c_2\hat{A}\psi_2$

Postulate 3. In any measurement of an observable A, associated with an operator \hat{A} , the only possible results are the eigenvalues a_n , which satisfy an eigenvalue equation

$$\hat{A}\psi_n = a_n \, \psi_n$$

Postulate 4. For a system in a state described by a normalized wave function Ψ , the average or expectation value of the observable corresponding to A is given by

$$\langle A \rangle = \int \Psi^* \, \hat{A} \, \Psi \, d\tau$$

Postulate 5. The wavefunction of a system evolves in time in accordance with the time-dependent Schrödinger equation

$$i\hbar \frac{\partial \Psi}{\partial t} = \hat{H} \Psi$$

$$\hat{H} = -\frac{\hbar^2}{2m} \frac{\mathrm{d}^2}{\mathrm{d}x^2} + V(x)$$

In 1D for a particle moving in a potential V(x)

Thank You

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